

**APPENDIX. Overview of the expectation maximization (EM) algorithm used to update conditional probabilities.**

The EM algorithm (Dempster et al. 1977) updates conditional probability values from case data by integrating over missing variables and their values. For example, consider the probability  $P$  of habitat variable  $x_1$  and population variable  $x_2$ . The joint probability of habitat and population occurrence is a product of the conditional probability of the population given the habitat conditions, and the unconditional probability of the habitat conditions, or  $P(x_2, x_1) = P(x_2 | x_1)P(x_1)$ . Further, define the probability of absence of habitat as  $P(x_1 = 0) = \alpha$ , the probability of a zero population given absence of habitat as  $P(x_2 = 0 | x_1 = 0) = \beta_1$ , and the probability of a zero population given presence of habitat as  $P(x_2 = 0 | x_1 = 1) = \beta_2$ . Then, the overall probability of occurrence of habitat and

population is the joint function  $L = \prod_{i=1}^m P(x_2 = x_{2i}, x_1 = x_{1i})$ , and the maximum likelihood function is  $\max(L) \forall \alpha, \beta_1, \beta_2$ .

The EM algorithm is useful when a specific condition  $x_L$  is not observed so that the joint probability distribution  $P(x_L, x_1)$  cannot be explicitly calculated. Instead, it can be estimated by integrating out  $x_2$  over the domain (0,1) using  $\int P(x_2, x_1) dx_2 = P(x_1)$ . This yields the marginal (unconditional) probability distribution over  $x_1$ , in other words, the marginal likelihood calculation. This calculation is used as the basis for updating the joint (and thus conditional) probabilities in the Bayesian network.